Sebastian Haratyk

October 23, 2015

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Biomathematics? What's that all about?

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Biomathematics is an interdisciplinary scientific research field, concerned with developing mathematical methods for biological purposes and applying mathematics to biological researches.

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Mathematical models are an abstract entities described by mathematical language which are used to reflect surrounding us world with events occurring in it and also to predict the future behaviours of systems.

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Epidemic models SIR and SIS models

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• S - group of susceptible and healthy individuals;

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Population models Ecological population models

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$$N_{n+1}=N_n+B_n-D_n-E_n+I_n,$$

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where:

• N_n - size of population at time t_n;

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Population models

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Predator-prey models

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Image: A mathematical states and a mathem

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Predator-prey models

These models are frequently used to describe the dynamics of biological systems in which two species interact, one as a predator and the other as prey.

Population models

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The most popular of predator-prey models is the one described by Lotka-Volterra equations.

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Population models

Models of plankton dynamics

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Population models

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Plankton are a diverse group of organisms that live in the water column of large bodies of water and that cannot swim against a current. They provide a crucial source of food to many large aquatic organisms, such as fish and whales.

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Plankton could be divided into:

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Plankton are a diverse group of organisms that live in the water column of large bodies of water and that cannot swim against a current. They provide a crucial source of food to many large aquatic organisms, such as fish and whales.

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- Zooplankton (animal plankton)

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Population models Models of plankton dynamics

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Image: A mathematical states of the state

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J.H. Steele and E. W. Henderson (1981) : *A simple plankton model* , The American Naturalist, **Vol. 117**, 676-691

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$$\frac{dN}{dt} = -\text{uptake} + \text{excretion} + \text{added } N,$$
$$\frac{dP}{dt} = \text{growth}(P) - \text{grazing} - \text{sinking} - \text{mixing},$$
$$\frac{dZ}{dt} = \text{growth}(Z) - \text{predation}.$$

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$$\begin{cases} \frac{dP}{dt} = \beta P(1 - \frac{P}{K}) - \frac{P}{P+1}Z\\ \frac{dZ}{dt} = \gamma \frac{P}{P+1}Z - \delta Z, \end{cases}$$

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• K - environment capacity coefficient,

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Population models

PZ Model

• If $\gamma \in (\frac{\delta(K+1)}{K}, \frac{\delta(K+1)}{K-1})$, then quantity of phyto- and zooplankton in our ecosystem tends to a critical point with positive coordinates - conditions of coexistence.

Population models

PZ Model

• If $\gamma \in (\frac{\delta(K+1)}{K}, \frac{\delta(K+1)}{K-1})$, then quantity of phyto- and zooplankton in our ecosystem tends to a critical point with positive coordinates - conditions of coexistence.



$$\beta = 0.5, \ \delta = 0.2, \ \gamma = 0.35, \ K = 5$$

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If γ < δ(K+1)/K then after some time whole population of zooplankton will extinct and the phytoplankton population size will stabilise on a constant magnitude equal to environment capacity coefficient K.

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Is that it?

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